

	Elements	$Q(x, y, y_x) = 0$	Solutions	Type Solution
1	Π_4	$(0) - y_x(x^3 y^2) = 0$	$y(x) = 0, y(x) = c$	Trivial
2	Π_2	$(0) - y_x(x^3) = 0$	$y(x) = c$	Trivial
3	Π_3	$(-y^3) - y_x(x y^2) = 0$	$y(x) = \frac{c}{x}$	Explicit
4	$\Pi_1 + \Pi_3$	$(-y^3) - y_x(x + x y^2) = 0$	$y(x) = \pm \frac{1}{\sqrt{W(x^2 c)}}$, with $W(z)$ the product log function.	Explicit
5	$\Pi_2 + \Pi_3$	$(-y^3) - y_x(x^3 + x y^2) = 0$	$y(x) = \pm \sqrt{\frac{e^{4c} c}{x^2} - \frac{\sqrt{e^{4c}(e^{4c} + x^4)}}{x^2}}$	Explicit
6	$\Pi_3 + \Pi_4$	$(-y^3) - y_x(x^3 y^2 + x y^2) = 0$	$y(x) = \frac{c\sqrt{x^2 + 1}}{x}$	Explicit
7	$\Pi_1 + \Pi_4$	$(0) - y_x(x + x^3 y^2) = 0$	$y(x) = \pm \frac{i}{x}, y(x) = c$	Explicit
8	$\Pi_2 + \Pi_4$	$(0) - y_x(x^3 + x^3 y^2) = 0$	$y(x) = \pm i, y(x) = c$	Explicit
9	$\Pi_3 + \Pi_5$	$(-y^3 + y) - y_x(x y^2) = 0$	$y(x) = \pm \frac{\sqrt{c + x^2}}{x}$	Explicit
10	$\Pi_2 + \Pi_5$	$(y) - y_x(x^3) = 0$	$y(x) = c e^{-1/(2x^2)}$	Explicit
11	$\Pi_1 + \Pi_5$	$(y) - y_x(x) = 0$	$y(x) = cx$	Explicit
12	$-2\Pi_1 + \Pi_4 + \Pi_5$	$(y) - y_x(x^3 y^2 - 2x) = 0$	$y(x) = \pm \frac{\sqrt{\pm \frac{e^{-2c} \sqrt{4e^{2c} + x^2}}{x} - e^{-2c}}}{\sqrt{2}}$	Explicit
13	$\Pi_2 + \Pi_3 + \Pi_4$	$(-y^3) - y_x(x y^2 + x^3 + x^3 y^2) = 0$	$y(x) = \pm \frac{1}{4} \sqrt{-\frac{1}{cx^2} \pm \frac{\sqrt{(x^2 + 1)^2 - 16cx^4}}{cx^2}} - \frac{1}{c}$	Explicit
14	$\Pi_1 + \Pi_2 + \Pi_4$	$(0) - y_x(x^3 + x^3 y^2 + x) = 0$	$y(x) = \pm \frac{\sqrt{-x^2 - 1}}{x}, y(x) = c$	Explicit
15	$\Pi_2 + \Pi_3 + \Pi_4 + \Pi_5$	$(y - y^3) - y_x(x^3 y^2 + x^3 + x y^2) = 0$	$\frac{1}{4} \left(\frac{1}{1 - y(x)^2} + \log 9 y(x) - \frac{1}{2} \log(1 - y(x)^2) \right) - \frac{1}{8x^2(y(x)^2 - 1)} = c$	Implicit