

Structural model of a piezo engine for composite telescope

Abstract

The structural model of a piezo engine for composite telescope is constructed. This structural model clearly shows the conversion of electrical energy by a piezo engine into mechanical energy of the control element of a composite telescope. The structural scheme of a piezo engine is determined. For the control systems with a piezo engine its deformations are obtained in the matrix form. This structural model, structural scheme and matrix equation of a piezo engine are applied in calculation the parameters of the control systems for composite telescope.

Keywords: Piezo engine, Structural model, Structural scheme, Matrix equation, Deformation, Composite telescope

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Introduction

A piezo engine based on the piezoelectric effect is used in the control systems for composite telescope and adaptive optics.¹⁻¹⁴ A piezo engine is applied for precise adjustment, compensation the deformations of composite telescope and scanning microscope.¹⁵⁻²¹ For decisions the displacements and the forces of a piezo engine in the control systems for composite telescope is used the structural model of a piezo engine. The structural model clearly shows the conversion of electrical energy by a piezo engine into mechanical energy of the control element of a composite telescope with using the physical parameters of a engine and its load.¹⁶⁻²⁸ The structural model and the structural scheme of a piezo engine for composite telescope are determined in difference from Cady's and Mason's electrical equivalent circuits of a piezo transducer.⁷⁻²⁸

Structural scheme of a piezo engine

The matrix state equations [8, 11-17] of a piezo engine have the form

$$\begin{aligned} (D) &= (d)(T) + (\varepsilon^T)(E) \\ (S) &= (s^E)(T) + (d^t)(E) \end{aligned}$$

where (D) , (S) , (T) , (E) are the matrices of electric induction, relative deformation, mechanical field and electric field stresses, and t is transpose operator. For PZT engine the matrices have the form

$$(d) = \begin{pmatrix} 0 & 0 & 0 & 0 & d_{15} & 0 \\ 0 & 0 & 0 & d_{15} & 0 & 0 \\ d_{31} & d_{31} & d_{33} & 0 & 0 & 0 \end{pmatrix}$$

$$(d^t) = \begin{pmatrix} 0 & 0 & d_{31} \\ 0 & 0 & d_{31} \\ 0 & 0 & d_{33} \\ 0 & d_{15} & 0 \\ d_{15} & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$(\varepsilon^T) = \begin{pmatrix} \varepsilon_{11}^T & 0 & 0 \\ 0 & \varepsilon_{22}^T & 0 \\ 0 & 0 & \varepsilon_{33}^T \end{pmatrix}$$

$$(s^E) = \begin{pmatrix} s_{11}^E & s_{12}^E & s_{13}^E & 0 & 0 & 0 \\ s_{12}^E & s_{11}^E & s_{13}^E & 0 & 0 & 0 \\ s_{13}^E & s_{13}^E & s_{33}^E & 0 & 0 & 0 \\ 0 & 0 & 0 & s_{55}^E & 0 & 0 \\ 0 & 0 & 0 & 0 & s_{55}^E & 0 \\ 0 & 0 & 0 & 0 & 0 & 2(s_{11}^E - s_{12}^E) \end{pmatrix}$$

The equation of the reverse piezo effect [8-51] has the form

$$S_i = d_{mi} E_m + s_{ij}^E T_j$$

where m, i, j are axes.

For the longitudinal piezo engine on Figure 1 its parameters are determined in the form

$$\Delta \delta_{\max} = d_{33} E_3 \delta = d_{33} U, F_{\max} = d_{33} E_3 S_0 / s_{33}^E$$

At $d_{33} = 4 \cdot 10^{-10}$ m/V, $E_3 = 0.8 \cdot 10^5$ V/m, $\delta = 2.5 \cdot 10^{-3}$ m, $S_0 = 1.5 \cdot 10^{-4}$ m², $s_{33}^E = 15 \cdot 10^{-12}$ m²/N its maximum values of deformation and force are received in the form $\Delta \delta_{\max} = 80$ nm, $F_{\max} = 320$ N with error 10%.

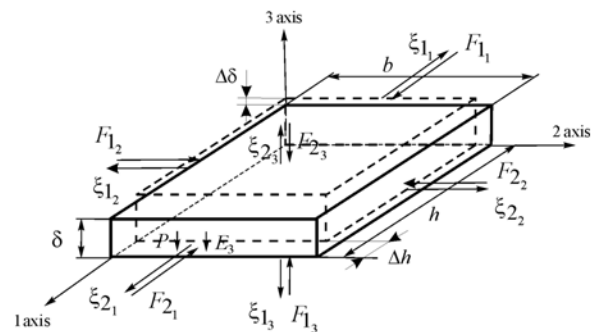


Figure 1 A piezo engine for composite telescope.

The differential equation for a piezo engine has the form^{11–51}

$$\frac{d^2 \Xi(x, s)}{dx^2} - \gamma^2 \Xi(x, s) = 0$$

where x, s, γ are coordinate, operator and coefficient.

Its solution has form

$$\Xi(x, s) = \{ \Xi_1(s) \text{sh}[(l-x)\gamma] + \Xi_2(s) \text{sh}(x\gamma) \} / \text{sh}(l\gamma)$$

For the stresses acting on two faces a piezo engine its transforms of Laplace have the form

$$T_j(0, s) = \frac{1}{s_{ij}^\Psi} \frac{d\Xi(x, s)}{dx} \Big|_{x=0} - \frac{d_{mi}}{s_{ij}^\Psi} \Psi_m(s)$$

$$T_j(l, s) = \frac{1}{s_{ij}^\Psi} \frac{d\Xi(x, s)}{dx} \Big|_{x=l} - \frac{d_{mi}}{s_{ij}^\Psi} \Psi_m(s)$$

where $\Psi = E$ or $\Psi = D$.

For the structural model and scheme of a piezo engine for composite telescope on Figure 2 its equations have the form

$$\Xi_1(s) = \left[1 / (M_1 s^2) \right] \left\{ -F_1(s) + (1 / \chi_{ij}^\Psi) \left[\frac{d_{mi} \Psi_m(s) - [\gamma / \text{sh}(l\gamma)]}{\times [\text{ch}(l\gamma) \Xi_1(s) - \Xi_2(s)]} \right] \right\}$$

$$\Xi_2(s) = \left[1 / (M_2 s^2) \right] \left\{ -F_2(s) + (1 / \chi_{ij}^\Psi) \left[\frac{d_{mi} \Psi_m(s) - [\gamma / \text{sh}(l\gamma)]}{\times [\text{ch}(l\gamma) \Xi_2(s) - \Xi_1(s)]} \right] \right\}$$

where $v_{mi} = \begin{cases} d_{33}, d_{31}, d_{15} \\ g_{33}, g_{31}, g_{15} \end{cases}$, $\Psi_m = \begin{cases} E_3, E_1 \\ D_3, D_1 \end{cases}$, $s_{ij}^\Psi = \begin{cases} s_{33}^E, s_{11}^E, s_{55}^E \\ s_{33}^D, s_{11}^D, s_{55}^D \end{cases}$,

$l = \{ \delta, h, b, \gamma = \{ \gamma^E, \gamma^D, c^\Psi = \{ c^E, c^D, \chi_{ij}^\Psi = s_{ij}^\Psi / S_0, v_{mi}$ is the piezo coefficient.

$$\xi_1(\infty) = d_{33} U M_2 / (M_1 + M_2)$$

$$\xi_2(\infty) = d_{33} U M_1 / (M_1 + M_2)$$

At $d_{33} = 4 \cdot 10^{-10}$ m/V, $U = 250$ V, $M_1 = 1$ kg and $M_2 = 4$ kg its displacements are obtained $\xi_1(\infty) = 80$ nm, $\xi_2(\infty) = 20$ nm, $\xi_1(\infty) + \xi_2(\infty) = 100$ nm with error 10%.

For the transverse piezo engine at elastic–inertial load the expression has the form

$$W(s) = \frac{\Xi(s)}{U(s)} = \frac{d_{31} h / \delta}{(1 + C_l / C_{11}^E) (T_i^2 p^2 + 2 T_i \xi_i p + 1)}$$

$$T_i = \sqrt{M / (C_l + C_{11}^E)}, \quad \omega_i = 1 / T_i$$

where C_l, C_{11}^E are the stiffness of load and engine, T_i, ξ_i, ω_i are the time constant, the attenuation coefficient and the conjugate

frequency of the engine. At $M = 3$ kg, $C_l = 0.2 \cdot 10^7$ N/m, $C_{11}^E = 1 \cdot 10^7$ N/m its parameters are determined in the form the time constant $T_i = 0.5 \cdot 10^{-3}$ s and the conjugate frequency of the engine $\omega_i = 2 \cdot 10^3$ s⁻¹ with error 10%.

Conclusion

The structural model of a piezo engine for composite telescope is obtained. The structural model clearly shows the conversion of electrical energy by a piezo engine into mechanical energy of the control element of a composite telescope using the physical parameters of a piezo engine and its load. The structural scheme of a piezo engine for composite telescope is determined.

The matrix equation of a piezo engine is received for the calculation its displacements and parameters. The structural model, the structural scheme and the matrix equation of a piezo engine are used in decisions of the control systems for composite telescope.

Acknowledgments

None.

Conflicts of Interest

None.

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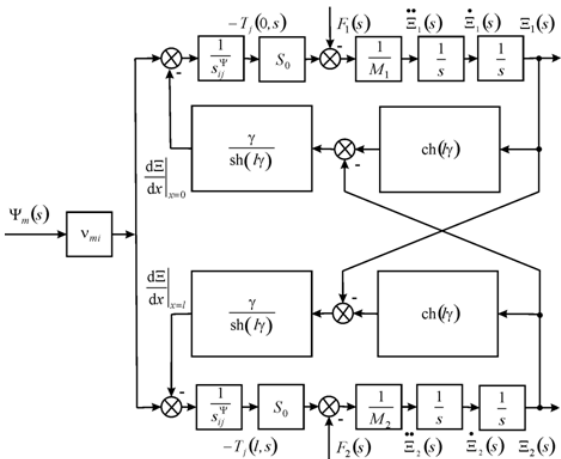


Figure 2 Structural scheme of a piezo engine for composite telescope.

Therefore, the matrix equation of a piezo engine has the form

$$\begin{pmatrix} \Xi_1(s) \\ \Xi_2(s) \end{pmatrix} = \begin{pmatrix} W_{11}(s) & W_{12}(s) & W_{13}(s) \\ W_{21}(s) & W_{22}(s) & W_{23}(s) \end{pmatrix} \begin{pmatrix} \Psi_m(s) \\ F_1(s) \\ F_2(s) \end{pmatrix}$$

The steady–state displacements of faces 1 and 2 for the longitudinal piezo engine have the form.

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