

New interpretation of the table of eclipses in Dresden Codex: Intercalated numbers as fractions

Abstract

A review to the introductory pages of the Table of Eclipses of the Dresden Codex is made. In particular, the section of three intercalated Maya numbers in columns A, B, C, of page 52a and the list of thirteen 13's (two bars and three points) present in column D of the same page are studied and interpreted as a way to construct the sequence of 69 eclipse prediction numbers for a total period of 11.958 days. Those intercalated numbers (red & black) in the codex represent big numbers that are multiples of the 11.960-day period. In combination with the draconic month (as studied by Chinese culture (27,2122)), the sequence of 177, 178, 148 days, intervals can be reproduced. The consequent conclusion is that these intercalated numbers could represent numerical fractions.

Keywords: maya numbers, fractional numbers, eclipse prediction, moon's latitude

Volume 8 Issue 2 - 2023

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Received: May 21, 2023 | **Published:** June 02, 2023

In this letter, I am presenting a possible interpretation of the intercalated numbers written in the section of aperture of the Table of Eclipses that are present in the page 52a of Dresden Codex. This new interpretation suggests that Maya Mathematics has made the use of fractions while generating the table for eclipse prediction inscribed in pages 53a to 58a and following from 51b through 58b. Also, a possible procedure to have the sequence of lunations will be discussed.

The Dresden Codex is one of the four original codices attributed to the Maya Culture before the arrival of Spaniards. The other three are: Paris Codex, Madrid Codex and Maya Codex, which was known as the Grolier Codex.¹ It is also, the codex having the greatest number of astronomical features.² For example, the Table of Venus, the Table of Mars and the lunar cycles, are some of the most important ones. The Table of Eclipses is the main issue analysed here.

The Dresden Codex is a folded book made of amate paper, covered by a thin layer of stucco in order to give a surface apt for writing. It has been accepted that the writing is in original Mayan hieroglyphic language, and it has 39 leaves, most of them are painted on both sides. The size of each leaf is 20,4 cm height by 9,0 cm wide; the total length of the codex is 3,50 m. Its name comes from the fact that it is conserved at the Saxony State Library in Dresden, Germany.²

In Figure 1A, it can be seen the page of interest for this proposal: 52a. There are several columns with hieroglyphic text at the top of it that can be read partially. The maya numbers present in the middle part of the first three columns are count of days as stated by Erik Velazquez in his interpretation. In Figure 1B, a schematic description of the page is given following the analysis made by Bricker. It is of highest interest to look at them and at the 13 13's in the central column. The three intercalated pairs of numbers adjacent to it have been deciphered due to its colours: Red and Black.

As it can be seen in the figure, the six numbers of the three columns are related with the whole extent of the table: the number of days reach multiples of 11.960 (rounding total of 11.958 corresponding to 69 predicted eclipses). I will come back to these numbers ahead. For the moment, the series of 13's has been interpreted as a way to recycle the table but without any mention a possible way to use it: Eric Velasquez says that "As Bricker and Bricker (2011) say, the rest of the sentence is a number of 1.828 days (5.1.8), which serves to update the table and be able to use it in the future, leading to new start dates, the same function that they attribute to the thirteen red numbers 13 located in

the lower half of this column" (2016: 74). Other interpretations of this column of 13's refers to a very big number (13 levels meaning an infinite) or as the thirteen levels of the world incorporated in the Maya cosmovision.



(a)

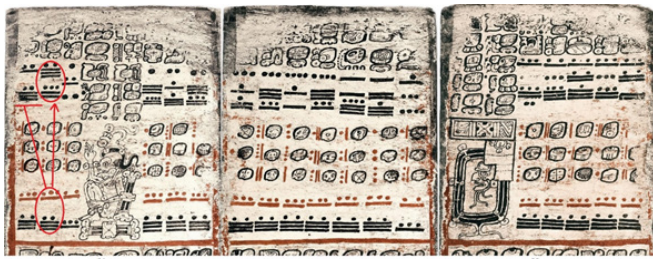
52aA	52aB	52aC	52aD	52aE	52aF
caption B R	caption B R	caption B R	caption 8 8ix 1 uinal 5 tun 2 ta-b(a) (+)	(4) Ahau 8 Cumku	(4 Ahau) 8 Cumku
3 (=4) 19 11 (=12) 0	3 6 11,960 0	4 8 11,960 0	6 18 11,960 0	=1,828 13 13 13 13 13 13 13	R R R R 9 9 9 9 16 19 16 16 4 8 4 4 10 (=11) 7 10 11 18 8 8 3
12 Lamat 1 Akbal 3 Edznab 5 Ben 7 Lamat	12 Lamat 1 Akbal 3 Edznab 5 Ben 7 Lamat	12 Lamat 1 Akbal 3 Edznab 5 Ben 7 Lamat	12 Lamat 1 Akbal 3 Edznab 5 Ben 7 Lamat		3 Edznab 7 Lamat 12 Lamat 1 Akbal

Note: Columns are labelled with upper-case letters, from left to right on each page. The black (B) and red (R) numbers that are here shown separately are shown alternately (interwined) within the same column on the Codex page (see fig. 1).

(b)

Figure 1 Contents of page 52a: a) Facsimile of the original codex;² b) Section of Table 1 of the schematic deciphered contents of the page.⁷

From page 53(a) to 58(b) there are a total of 79 columns (69 numeric plus 10 including figures), for my proposal, only the sections of the black number that represents the number of days accumulated from the beginning column of the table and the number corresponding to 177 or 148, which in Mayan notation are written (8.17) and (7.8), respectively, in the lower part of each column (see Figure 2A. In several places, the cumulative total reaches a number that assumes a 178 has been added but in the lower part a 177 is written: the sequence of lapses' days for the occurrence of an eclipse could be, only, 177, 178 or 148³ as it can be seen in Figure 3B.



Intervalos (días)	Figura	Total (días)
177, 177, 148	53a	502
177, 177, 177, 177*, 177, 177, 177, 177, 148	55a	1,734
177*, 177, 177, 177, 177, 148	56a	1,034
177, 177, 177, 177*, 177, 177, 148	57a	1,211
177, 177, 177*, 177, 177, 177, 177, 177, 148	52b	1,742
177*, 177, 177, 177, 177, 148	53b	1,034
177, 177, 177, 177, 177, 177, 148	54b	1,210
177, 177, 177*, 177, 177, 177, 177, 177, 148	56b	1,565
177, 177*, 177, 177, 177, 177, 148	57b	1,211
177, 177, 177, 177	58b	708

Nota: *en ocasiones se suma 178 aunque el número anotado es 177

(b)

Figure 2 Lapses of days for the occurrence of an eclipse in Dresden Codex: a) Part of the facsimile pages (53a, 54a, 55a),² with accumulation in Red; b) sequence of 69 intervals of days.³

It can be probed, as I myself do in another paper, that the dates corresponding to the sequence of 177, 178, and 148 days, lapses can be correlated with eclipses observed at somewhere on Earth, not necessarily in the zone of Maya influence.^{3,4}

I now ask the critical question about the Table of Eclipses of Dresden Codex: Is there any relation between the information in page 52a, mainly the list of 13's and the multiples of 11.960, and the sequence of intervals of Figure 3B? Any of the many studies have addressed ideas towards this question.^{5,6}

In order to give a possible answer to this matter, I will discuss briefly the lunar observations made in ancient China. Christopher Cullen has published a very interesting book, "Heavenly Numbers" (2021), about the astronomy in the early imperial China. I am using the Table of Ying-Yang Sequence shown in Table 1. The contents of the table give us a very important information about what is called the Draconic month: a cycle of 27.212220 days taken by the Moon to make two passages through the same node (intersection of its orbit with the ecliptic).

The column 1 gives the number of days for the Moon being above or below the ecliptic, because the angle between the orbit of the Moon and the ecliptic is about 6 du, which means that the alignment of the three celestial bodies (Earth, Moon and Sun) and, in consequence, the propitious moment for an eclipse (lunar or solar) is of 13 days and a fraction. The corresponding fractions shown in last row of the table are, for a whole cycle 0,13363 and 0,64693. In the real world both fractions change due to several astronomical factors like precession or tidal forces. The reported ones are long term means.

The extension in space of the Moon and Sun makes possible three types of solar eclipses: partial, annular and total.

Table 1 Uranic manifestation system Ying-Yang sequence

1	2	3	4
Day of Ying-Yang sequence	Difference [1/12 du]	Rate of Decrease and Increase [1/12du]	Total Number [1/12 du]
1	-1	17	0
2	-1	16	17
3	-3	15	33
4	-4	12	48
5	-4	8	60
6	-3	4	68
7	-3	1	72
8	4	-2	73
9	4	-6	71
10	3	-10	65
11	2	-13	55
12	1	-15	42
13	1	-16	27
Fractional day [5203/77874 days]		-(16[+306/473])	11

The number thirteen (13 or two bars and three points) becomes relevant to the observation of the latitude of the Moon. Let me show how the 13's and a fraction could work to obtain the sequence of 69 intervals of the table shown in Figure 2B.

The first thing to notice is that summing 13 13's we arrive to 169 days. Then we can assume that column D of page 52a (see Figure 1B) make a base of 169 that need 8 days to arrive to 177 and 9 days to arrive to 178. In Table 2, I show the fractions needed to generate the three lunation cycles for an eclipse, assuming that the fractions are the same for all the periods.

Table 2 Lunations for eclipse observation

Number	13	13	13
Times	13	13	11
Base	169	169	143
Fraction	0.61538	0.69231	0.45455
Total	177	178	148

Table 3 Lunations using fractions from Dresden Codex*

Number	13	13	13
Times	13	13	11
Base	169	169	143
Fraction**	0.6	0.66667	0.28804
Total	176.8	177.67	146.17

*Table of Eclipses page 52a

**Ratio between Black and Red numbers of cols. A, B, C of the same page, respectively

The proper application of this table 3 would allow to reproduce the whole 69 intervals of the sequence; however, if one think about an alternative and nonhomogeneous way to arrive to it, it is possible to assign (observed?) fractions to the sequence. This is why I have look forward to the intercalated numbers in columns A, B, C, of page 52a

(see Figure 1B). Taking the ratio between Black and Red numbers, we arrive to the following three fractions: $3/5$; $2/3$; and $0,28804$.

My interpretation of these B&R numbers on the Dresden Codex because they are not exact, would imply that in constructing the table, some observational criteria could have been used as it is shown in an alternative reconstruction of the sequence of Table 4.

I can conclude with these words: In one of the introductory pages (52a) of the Table of Eclipses of the Dresden Codex, the list of 13 13's in Column D, can be used coupled to the intercalated B&R numbers of columns A, B, C, representing fractions, to elaborate the sequence of lunations (intervals of 177, 178, 148 days) on the remaining pages of the table.

Table 4 An alternative way to build the intervals sequence

Serie	Acc	Serie	Acc	Serie	Acc	Serie	Acc	Serie	Acc
13.600	13.6	13.667	1183.4	13.600	1810.0	13.667	2421.0	13.667	2925.6
13.600	27.2	13.667	1197.0	13.600	1823.6	13.600	2434.6	13.667	2939.2
13.600	40.8	13.667	1210.7	13.600	1837.2	13.600	2448.2	13.667	2952.9
13.600	54.4	13.600	1224.3	13.600	1850.8	13.600	2461.8	13.600	2966.5
13.600	68.0	13.667	1238.0	13.600	1864.4	13.600	2475.4	13.600	2980.1
13.600	81.6	13.600	1251.6	13.600	1878.0	13.600	2489.0	13.600	2993.7
13.600	95.2	13.667	1265.2	13.667	1891.7	13.600	2502.6	13.600	3007.3
13.600	108.8	13.600	1278.8	13.667	1905.4	13.600	2516.2	13.600	3020.9
13.667	122.5	13.667	1292.5	13.667	1919.0	13.600	2529.8	13.600	3034.5
13.600	136.1	13.600	1306.1	13.600	1932.6	13.600	2543.4	13.600	3048.1
13.667	149.7	13.600	1319.7	13.600	1946.2	13.667	2557.0	13.667	3061.8
13.600	163.3	13.600	1333.3	13.600	1959.8	13.600	2570.6	13.600	3075.4
13.667	177.0	13.667	1347.0	13.600	1973.4	13.667	2584.3	13.600	3089.0
13.600	190.6	13.667	1360.6	13.600	1987.0	13.667	2598.0	13.667	3102.6
13.600	204.2	13.667	1374.3	13.600	2000.6	13.667	2611.6	13.667	3116.3
13.600	217.8	13.667	1388.0	13.600	2014.2	13.667	2625.3	13.667	3130.0
13.600	231.4	13.600	1401.6	13.600	2027.8	13.667	2639.0	13.600	3143.6
13.600	245.0	13.600	1415.2	13.600	2041.4	13.667	2652.6	13.600	3157.2
13.600	258.6	13.600	1428.8	13.600	2055.0	13.667	2666.3	13.288	3170.5
13.600	272.2	13.600	1442.4	13.667	2068.7	13.667	2680.0	13.600	3184.1
13.600	285.8	13.600	1456.0	13.667	2082.4	13.667	2693.6	13.600	3197.7
13.667	299.5	13.600	1469.6	13.667	2096.0	13.667	2707.3	13.288	3210.9
13.600	313.1	13.600	1483.2	13.288	2109.3	13.667	2721.0	13.600	3224.5
13.667	326.7	13.600	1496.8	13.667	2123.0	13.667	2734.6	13.288	3237.8
13.600	340.3	13.600	1510.4	13.600	2136.6	13.667	2748.3	13.600	3251.4
13.667	354.0	13.600	1524.0	13.600	2150.2	13.667	2762.0	13.288	3264.7
13.600	367.6	13.667	1537.6	13.667	2163.9	13.667	2775.6	13.288	3278.0
13.600	381.2	13.667	1551.3	13.288	2177.1	13.600	2789.2	148.0	
13.288	394.5	13.667	1565.0	13.288	2190.4	13.667	2802.9		
13.600	408.1	13.600	1578.6	13.667	2204.1	13.600	2816.5		
13.600	421.7	13.600	1592.2	13.288	2217.4	13.600	2830.1		
13.600	435.3	13.600	1605.8	13.288	2230.7	13.667	2843.8		
13.288	448.6	13.600	1619.4	13.288	2244.0	13.600	2857.4		
13.600	462.2	13.600	1633.0	13.600	2257.6	13.600	2871.0		
13.288	475.5	13.600	1646.6	13.600	2271.2	13.667	2884.6		
13.288	488.8	13.600	1660.2	13.600	2284.8	13.600	2898.2		
13.288	502.0	13.600	1673.8	13.600	2298.4	13.667	2911.9		
13.600	515.6	13.600	1687.4	13.600	2312.0				
13.600	529.2	13.667	1701.0	13.600	2325.6				
13.600	542.8	13.667	1714.7	13.600	2339.2				
13.600	556.4	13.667	1728.4	13.600	2352.8				
13.600	570.0	13.667	1742.0	13.600	2366.4				
13.600	583.6	13.600	1755.6	13.600	2380.0				
13.600	597.2	13.600	1769.2	13.667	2393.6				
13.600	610.8	13.600	1782.8	13.667	2407.3				
13.600	624.4	13.600	1796.4						
13.600	638.0								
13.600	651.6								
13.667	665.3								
13.667	679.0								
13.600	692.6								
13.600	706.2								
13.600	719.8								
13.600	733.4								
13.600	747.0								
13.600	760.6								
13.600	774.2								
13.600	787.8								
13.667	801.4								
13.600	815.0								
13.667	828.7								
13.600	842.3								
13.667	856.0								
13.600	869.6								
13.600	883.2								
13.600	896.8								
13.600	910.4								
13.667	924.0								
13.600	937.6								
13.667	951.3								
13.600	964.9								
13.667	978.6								
13.600	992.2								
13.600	1005.8								
13.667	1019.4								
13.600	1033.0								
13.667	1046.7								
13.667	1060.4								
13.667	1074.0								
13.667	1087.7								
13.667	1101.4								
13.667	1115.0								
13.667	1128.7								
13.667	1142.4								
13.667	1156.0								
13.667	1169.7								

Col-Dresde	AccDresde	Col-Dresde	AccDresde	Col-Dresde	AccDresde
177	177	2421	177	177	7441
177	354	177	2598	177	7618
148	502	178	2776	177	7795
177	679	177	2953	177	7972
177	856	177	3130	177	8149
177	1033	148	3278	177	8326
178	1211	177	3455	148	8474
177	1388	177	3632	177	8651
177	1565	177	3809	177	8828
177	1742	177	3986	178	9005
177	1919	178	4164	177	9183
177	2096	177	4341	177	9360
148	2244	147	4488	177	9537
		177	4665	177	9714
		177	4842	177	9891
		178	5020	148	10039
		177	5197	177	10216
		177	5374	178	10394
		177	5551	177	10571
		177	5728	177	10748
		177	5905	177	10925
		177	6082	177	11102
		148	6230	148	11250
		178	6408	177	11427
		177	6585	177	11604
		177	6762	177	11781
		177	6939	177	11958
		177	7116		
		148	7264		

It follows to look forward for instructions to be made in order to have the correct sequence. The texts on the top of the columns must be interpreted accordingly.^{7,8}

Acknowledgements

I want to give thanks to the collaborators of the project of MAMH (Monumental Antikythera Mechanism for Hermosillo) for their useful comments: Ezequiel Rodríguez, Julio Saucedo, Alfredo Carmona, and J. Clemente Olvera. Also, my appreciation to Eduardo Rodas, Jesús Galindo and Stanislaw Iwaniszewski, for their critics and for being introduced in the field of Dresden Codex.

Conflicts of interests

Author declares there are no conflicts of interests.

Funding

None.

References

1. Chanier T. Solution of the mayan calendar enigma. *arXiv:1601.03132v7*. 2018.
2. Velásquez E. Codex Dresden Part 1. Facsimile Edition. *Mexican Archaeology*. 2016:8–100.
3. Marín D, Joshua L. The eclipse table in the Dresden codex: Over a hundred years of study and discussion. *Science, Technology and Health*. 2019;6(1):53–67.
4. Perez-Enriquez R. Comparison of the Mayan Eclipse Table and the Greek Saros Cycle. 2023.
5. Iwaniszewski S. The mayan lunar theory in astronomy in Mexico before and after the conquest. Susana Lizano and Luis Felipe Rodríguez Jorge, editors. *The National College Booklets*. 2022:57–84.
6. Teeple JD. Astronomia maya. *Anales. Bp. MT. II.-60*. 1960:479–581.
7. Bricker HM, Bricker VR, Aveni AF, et al. Classic maya prediction of solar eclipses [and Comments and Reply]. *Current Anthropology*. 1983;24(1):1–23.
8. Cullen Ch. Heavenly numbers: Astronomy and authority in early imperial China. *Oxford University Press*. 2017.