

**Research Article** 





# Evaluation of the productivity of vertical oil wells by using different high shot density (HSD) guns

# Abstract

This work explains how to evaluate the different perforation parameters of the production vertical oil wells by using well test reservoir description and perforation information. The necessary data have been collected from Hungarian oil wells including reservoir description data from the MOL Company files. Four vertical oil wells have been evaluated. The perforating guns data collected from the Schlumberger Company. Four perforating HSD guns were used with different charge and explosive load design.

In this study, calculation method used to determine the perforation depth, the influence of the different composite skin effect (damage skin factor, crushed zone skin factor, and the perforation skin factor), than we evaluate the flow rate of the different kind of guns. We consider the most important parameters influence the productivity of the perforated vertical oil wells. We obtained the relationship between the perforation depth and the skin factor, the perforation depth and the flow rate, the skin factor and the flow rate, and we identify the different flow rate. After giving the detailed figures and results, we evaluate the results of the perforation work.

In this work we proved that there is calculation method by which the flow rate of the vertical oil well can be estimated before the perforating. To have the best flow rate we should choose the right design of the perforation gun. Hungarian oil wells will improved their productivity by using high shut density guns. Flow rate evaluation needs a good knowledge of rock properties, and flow properties.

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# Introduction

Certainly, when a well has been cased and cemented a flow communication between the formations and wellbore must be provided, this contains creating a sequence of holes through casing and cement perforating. A lot of perforating guns are used in oil industry. Selecting the best perforation method is very important task during oil/gas well completion.

Skin Factor must be considered while perforating. The concept of skin factor initiates from Hurst work.<sup>1</sup> They proposed skin factor as a means to quantify non-ideal flow. Van Everdinen's<sup>2</sup> introduce the skin concept which includes two field examples that illustrate the use of skin to quantify formation damage and flow restriction due to perforation. These are the furthermost understandable causes of near-wellbore flow restriction.

The invading fluids and solids act together with the formation, creating a multitude of productivity damage effects, such as (emulsion blockage, water blockage, change in rock wet ability, hydration and swelling of formation clays, dispersion and migration of formation fines and grain cementation materials (clay particles), precipitation of inorganic salts (scaling), particle plugging of pores from entrained solids). The net effect of the invading fluid interaction with the formation is generally detrimental. The result is formation damage, causing additional pressure losses near the wellbore and a reduction in well productivity.

Regardless of the methods of damage prevention, there usually exists some degree of damage that must be considered in productivity calculations. The effect of formation damage on productivity has plagued the petroleum industry since its origin. It was treated systematically by Muskat,<sup>3</sup> using a model of a well producing from a formation with two concentric annular regions of different permeability. He notes that the physical model of discontinuous radial difference in the permeability corresponds to a well which was initially drilled into homogeneous sand, the in homogeneity having been caused by a partial plugging or mudding off of the region immediately surrounding the sand face during the course of production or in the process of drilling.

Most wells today are completed with production casing cemented in place and perforated to allow reservoir fluids to enter the wellbore. The current perforating techniques use shaped charges to produce penetrating jets, which perforate through the casing and the cement sheath. Flow through perforations affects the productivity of a well primarily by changing the local flow geometry near the wellbore.

The effect of perforations on well performance is usually expressed as a skin factor. In fact, Muskat<sup>4</sup> proposed the first appearance for perforation skin and discussed its similarity to an apparent wellbore radius. The specific geometrical parameters affecting the productivity of the perforated interval have been studied analytically by Muskat,<sup>4</sup> with analogy models by McDowell & Muskat<sup>5</sup> and Howard & Watson,<sup>6</sup> and with numerical simulators by Harris,<sup>7</sup> Hong,<sup>8</sup> & Locke.<sup>9</sup>

The Harris<sup>7</sup> study is one of the more comprehensive on the effect of perforation on productivity. Standing<sup>10</sup> rearranged the Harris's results into two handy charts. That give skin as a function of perforation depth beyond the casing (0 to 30 in.), density (1, 2, or 4 shots per foot), and phasing (0° or 180°). Standing notes that the 180° chart can also be used for 120° phasing, and work by Locke suggests that the 180° chart

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should also apply to 90° phasing without much error. According to Locke, Harris's skin factors are too large for shallow penetration and too small for deep penetration, but the differences are small.

Harris's work does not consider the possibility that formation damage exists near the wellbore. Intuitively, penetration that exceeds the depth of the damage significantly improves the inflow. It is impossible, however, to estimate the magnitude and the extent of formation damage after the well has been cleaned up by acid factor. The Standing-Harris curves are specifically for one-half-inch perforations through cemented casing in 9½-in. Wellbore (bit diameter). Therefore, we consider the perforation damage in our calculation to determine the flow rate for different vertical oil wells in Hungary by using a different high shut density guns.

# Methodology of this work

# High shot density (HSD) guns

In this work, we assume those wells producing only single oil phase. Thus, in our calculation we calculated what would be the flow rate for the examined well if the choosing perforation guns were used for those wells. We looked through the Schlumberger engineering perforation systems for the power jet, and we tried to select the best one of those guns. Regarding to our theoretical overview for the perforation guns, we choose the four different kind of high shot density guns (HSD) as following:-

Gun designation 2  $\frac{1}{2}$  in HSD: Charge 31 J CS, HMX, Maximum Explosive Load 10.7 g, (API: Penetration 19.2 in, Entrance Hole 0.30 in).

**Gun designation 2**  $\frac{7}{8}$  **in HSD:** Charge 34 J UJ, HSD, Maximum Explosive Load 15.2 g, (API: Penetration 20.6 in , Entrance Hole 0.29 in).

**Gun designation 2**  $\frac{7}{8}$  **7/8 in HSD:** Charge 34 J UJ, HMX, Maximum Explosive Load 15.0 g, (API: Penetration 22.0 in, Entrance Hole 0.30 in).

Gun designation 2  $\frac{7}{8}$  in HSD: Charge PJ 2906, HMX, Maximum Explosive Load 15.0 g, (API: Penetration 26.0 in, Entrance Hole 0.28 in).

# Skin factor and related concepts

The constant and rate-dependent skins are discussed in this section. Generally, we are interested only in the pseudo steady-state skin and can neglect the transience of the skin effect. This also applies to the high-velocity skin. Expressed in equation, skin is included the calculation of total pressure drop and flow rate for pseudo steady-state conditions in an oil well as:

$$q_{o} = \frac{kh(p_{R} - p_{wf})}{141.2\mu_{o}B_{o}\left[\ln(r_{e}/r_{w}) - 0.75 + s\right]}$$
(1)

Where pressure drop due to skin is expressed as

$$\Delta p_s = \frac{141.2q_o\lambda_oB_o}{Kh} S \tag{2}$$

Skin s is the composite of all non-ideal conditions affecting flow, the most important of which are

S<sub>d</sub>=formation-damage skin,

S<sub>e</sub>=completion skin due to partial penetration,

- S<sub>p</sub>=perforation skin,
- S<sub>b</sub>=blockage skin,
- S<sub>c</sub>=gravel-pack skin,
- S<sub>A</sub>=outer boundary geometry skin.

Craft & Hawkins<sup>11</sup> were the first to translate the Muskat model of a near-wellbore altered permeability into an expression for skin factor:

$$S_a = (k / k_a - 1) \ln (r_a - r_w)$$
 .....(3)

Where k is the formation permeability and  $k_a$  is the altered permeability extending from the wellbore radius  $r_w$  to a radius  $r_a$ . We select the subscript a denoting an altered permeability, rather than d denoting formation damage, to emphasize that equation (3) is valid also for cases of increased near-wellbore permeability (stimulation). A problem Inherent with the practical use of equation (3) is that the altered zone is very difficult to quantify in terms of  $k_a$  and  $r_a$ . That is, altered permeability and radius cannot be measured directly. At best, if the skin of the altered zone can be backed out of the total skin (calculated from well test analysis), an estimate of the radius of the altered zone  $r_a$  allows calculation of the altered-zone permeability, by simple rearrangement of equation (3).

Other expressions relating the skin to altered-zone permeability and radius are obtained by simple rearrangement of equation (3):

$$k_{a} = k \left[ 1 + \frac{S_{a}}{\ln(r_{a}/r_{w})} \right]^{-1}$$
 .....(4)

Solving for radius of the altered zone gives

$$r_a = r_w \exp\left[1 + \frac{S_a}{(k/k_a - 1)}\right]$$
(5)

Simplified expressions for the typical situation of a stimulated well when  $k_a >> k$  are

# Perforation penetration, geometry, and density

The most important parameters recognized by the studies are:-

**Penetration depth:** The deeper the penetration, the better the performance.

**Perforation diameter:** The larger the diameter of the perforation tunnel, the better the flow performance.

Shot density: The more shots per foot, the better the performance.

**Phasing:** The phasing, the angular pattern of shots around the wellbore, has an effect on productivity.

Thompson<sup>12</sup> has developed an empirical correlation relating perforation penetration to rock compressive strength. He gives a simple equation for estimating the correction from standard Berea penetration  $L_{pB}$  to actual penetration  $L_{p}$  (in):

Where

 $L_p$ =depth of penetration from the formation face (in.) (total core penetration=PTC)

 $L_{pB}$ =depth of penetration from the inside of the casing, through a 3/8-in. casing and <sup>3</sup>/<sub>4</sub>-in. cement sheath (in.) (total target penetration=TTP),

 $C_{\rm B}$  = Berea compressive strength  $\approx 6500$  Psia,

C= rock compressive strength (Psia),

Ts=cement sheath thickness (in.) (usually 0.75 in.),

Tc=casing thickness (in.) (usually 0.375 in.).

Several authors<sup>9,13</sup> suggest that the effect of a crushed zone can be quantified as a skin factor and included in IPR calculations. McLeod used a model of a "horizontal micro well" with formation damage around it as an analogy to a perforation surrounded by a crushed zone. His model gives the following relation for steady-state skin due to reduced crushed-zone permeability:

Where

K = formation permeability (md),

 $k_{dp}$  = crushed-zone permeability near the wellbore (md),

k<sub>a</sub> = damage-zone radius (in.),

 $r_{dp}$  = crushed-zone radius (in.),

 $r_{p}$  = perforation radius (in.),

 $L_{p}$  = depth of penetration (in.),

 $h_{n}$  = perforated interval (ft),

n = total number of perforations.

# **Composite skin factor**

Rowland,<sup>14</sup> & Jones & Watts<sup>15</sup> proposed simple models for adjusting individual skin factors for the effect of limited entry. In which flow convergence into the open interval is already completed before reaching the region where damage, high-velocity flow, blockage, and perforation effects become important. The higher local flow velocity magnifies the pressure drawdown caused by the other skin factors. Using the formal definition of skin factor and the h/hp gain in local velocity (in relation to ideal flow), pressure drawdowns corresponds to the ideal flow and the various skins. So finally consideration the above mention, the total different pressure can be calculated by the following equation:-

Where S is given by

And D is given by

$$D = D_{R} + D_{a} + D_{dp} + D_{G}$$
 .....(12)

Equation 11 and 12 are equally applicable to gas wells using pressure-squared, pressure, or pseudo-pressure. Note that  $S_C$ ,  $S_A$ ,  $S_G$ , and  $S_{dp}$  are not corrected for limited entry. This is because limited entry is inherently considered when these skin factors are calculated individually. A similar condition holds for the individual elements D.

# Consider the perforation skin effect by karakas and tariq

Karakas and Tariq (1988) have developed a procedure to calculate the skin effect due to perforations. This skin effect is a composite involving the plane-flow effect,  $S_h$ , the vertical converging effect,  $S_v$ , and the wellbore effect,  $S_{wh}$ , Hence

$$s_p = s_h + s_v + s_h \tag{13}$$

The pseudo skin factor, S<sub>h</sub>, is given by

$$s_{h} = \ln \frac{r_{w}}{r_{w}(\theta)} \tag{14}$$

Where  $r_{w}(\theta)$  is the effective wellbore radius and is function of the phasing angle  $\theta$ :

Where  $l_p$  is the length of the perforation and  $\alpha\theta$  is a phase dependent variable and can be obtained from Table 1.

**Table I** Depending of  $\alpha\theta$  on Phasing

Perforation phasing	$\alpha \theta$
0°(360°)	0.25
180°	0.5
120°	0.648
90°	0.726
60°	0.813
45°	0.86

The vertical pseudo skin factor, S<sub>v</sub>, Can be calculated after certain dimensionless variables are determined:

$$h_D = \frac{h}{l_p} \sqrt{\frac{k_h}{k_v}} \tag{16}$$

Where h is the distance between perforations and is exactly inversely proportional to the shot density  $k_h$  and  $k_v$  is the horizontal and vertical permeability's respectively;

$$r_{pd} = \frac{r_{perf}}{2h} \left(1 + \sqrt{\frac{k_v}{k_h}}\right) \tag{17}$$

Where  $r_{perf}$  is the perforation diameter, and

$$r_{wd} = \frac{r_w}{l_p + r_w} \tag{18}$$

The vertical pseudo skin effect is then given by

Where a and b are given by

$$a = a_1 \log r_{pD} + a_2 \tag{20}$$

$$b = b_1 + r_1 + b_2 \tag{21}$$

$$b = b_1 + r_{pD} + b_2 \tag{21}$$

The values of the constants  $a_1, a_2, b_1$ , and  $b_2$ , are given in Table 2 as functions of the phasing angle,  $\theta$ .

 Table 2
 Vertical Skin Correlation Coefficients

Phasing	a,	<b>a</b> <sub>2</sub>	Ь,	b <sub>2</sub>
0°(360°)	-2.091	0.0453	5.1313	1.8672
180°	-2.025	0.0943	3.0373	1.8115
120°	-2.018	0.0634	1.6136	1.777
90°	-1.905	0.1038	1.5674	1.6935
60°	-1.898	0.1023	1.3654	1.649
45°	-1.788	0.2398	1.1915	1.6392

Finally, the wellbore skin effect, s<sub>wb</sub>, can be approximated by

$$S_{wb} = C_1 e^{c_2 r_{wD}}$$

The constants  $c_1$  and  $c_2$  can be obtained from Table 3 **Table 3** Variables  $C_1$  and  $C_2$ .

Perforation phasing	C,	<b>C</b> <sub>2</sub>
0°(360°)	1.60E-01	2.675
180°	2.60E-02	4.532
120°	6.60E-03	5.42
90°	1.90E-03	6.155
60°	3.00E-04	7.509
45°	4.60E-05	8.791

# **General data of the wells**

We collected twelve wells data from the MOL Oil Company in Hungary and we choose four of them to study in this work. For those wells, we collected a well test evaluation report which was including some of the parameters which was necessary such as a reservoir description and fluid properties as well as the layer properties. The data which we used in the calculation model is shown in (Table 4-7). We made assumption in some of the data which wasn't including in the well test data and the perforation information. We couldn't get the perforation data from the MOL Oil Company. We made our assumption to many parameters depending on the Hungarian oil vertical well situation. We used some information from the Schlumberger design report. We assumed that the damage zone permeability equal to the formation oil permeability divided by five. The vertical permeability it usually equal to the damage zone permeability, and the horizontal permeability it is usually equal to the oil permeability. Our assumption were for some parameters such as (Radiuses of formation damage, Horizontal permeability, Vertical permeability, Damaged zone permeability, Crushed zone permeability, Crushed zone thickness). (Table 4-7) show the data for the well parameters matching of wells 1, 2, 3, and 4 including the reservoir description and the perforation information, respectively.

Table 4 The Basic Data for Well I

Parameters	Values
Formation thickness (ft)	26.2467
Reservoir pressure (psia)	2246.18
Flow Bottom hole pressure (psia)	2185.933
Oil viscosity (cp)	0.27377
Oil formation volume factor (bbl/STB)	1.37151
Reservoir permeability (mD)	169
Well radius (ft)	0.292
Drainage radius ft)	4969.245
Average Formation Porosity	0.3
Perforation interval (ft)	6.56
Rock compressive strength (calculated, psia)	4125.548
Perforation tunnel diameter for the different guns (1,2,3,4) (in)	0.30, 0.29, 0.30, 0.28
Perforation phasing , (°)	60
Shot density (shots/ft)	6
Crushed zone thickness (assumed, in)	0.5
Crushed zone permeability (assumed, mD)	5
Damaged zone permeability (assumed k/5, mD)	33.8
Vertical permeability (equal ka, mD)	33.8
Horezontal permeability (equal k,mD)	169
Radiused of formation damage (assumed ,ft)	1.375
Formation Temperature (deg F)	206.599

Table 5 The Basic Data for Well 2		Parameters	Values
Parameters	Values	Crushed zone thickness (assumed, in)	0.5
Formation thickness (ft)	19.685	Crushed zone permeability (assumed, mD)	5
Reservoir pressure (psia)	2347.91	Damaged zone permeability (assumed k/5, mD)	48.6
Flow Bottom hole pressure (psia)	2322.513	Vertical permeability (equal ka, mD)	48.6
Oil viscosity (cp)	0.67184	Horezontal permeability (equal k,mD)	243
Oil formation volume factor (bbl/STB)	1.25527	Radiused of formation damage (assumed ,ft)	1.375
Reservoir permeability (mD)	214	Formation Temperature (deg F)	201.469
Well radius (ft)	0.292	Table 7 The Basic Data for Well 4	
Drainage radius (ft)	4336.16	<b>D</b>	
Average Formation Porosity	0.32		
Perforation interval (ft)	3.28	Formation thickness (ft)	193.57
Rock compressive strength (calculated, psia)	4094.174	Reservoir pressure (psia)	2112.895
Perforation tunnel diameter for the different guns $(1,2,3,4)$ (in)	0.30, 0.29, 0.30, 0.28	Flow Bottom hole pressure (psia) Oil viscosity (cp)	0.39349
Perforation phasing , (°)	60	Oil formation volume factor (bbl/STB)	1.6428
Shot density (shots/ft)	6	Reservoir permeability (mD)	301
Crushed zone thickness (assumed, in)	0.5	Well radius (ft)	0.187
Crushed zone permeability (assumed, mD)	5	Drainage radius (ft)	1705.6
Damaged zone permeability (assumed k/5, mD)	42.8	Average Formation Porosity	0.07
Vertical permeability (equal ka, mD)	42.8	Perforation interval (ft)	32.8
Horezontal permeability (equal k,mD)	214	Rock compressive strength (calculated, psia)	4101.885
Radiused of formation damage (assumed ,ft)	1.375	Perforation tunnel diameter for the different $(1,2,2,4)$ (1)	0.30, 0.29, 0.30, 0.28
Formation Temperature(deg F)	194.319	guns $(1,2,3,4)$ (in)	<b>(</b> 0
Table 6         The Basic Data for Well 3		Shot density (chots/ft)	60
			0
Parameters	Values	Crushed zone thickness (assumed, in)	0.5
Formation thickness (ft)	4.9213	Crushed zone permeability (assumed, mD)	5
Reservoir pressure (psia)	2270.691	Damaged zone permeability (assumed k/5, mD)	60.2
Flow Bottom hole pressure (psia)	2226.469	Vertical permeability (equal ka, mD)	60.2
Oil viscosity (cp)	0.28194	Horezontal permeability (equal k,mD)	301

Table Continued....

# **Results and discussion**

Formation Temperature(deg F)

Radiused of formation damage (assumed ,ft)

Equation (1) was used to calculate the flow rate. Thomson method was used to calculate the perforation depth by using equation (8). To calculate the perforation depth, it was necessary to know the formation compressive strength. To calculation flow rate, we need to calculate the composite skin factor considering the equations number (3, 9, 11, and 13). We consider the effect of different parameters such as (damage zone skin factor, perforation skin factor, and crushed zone skin factor). We showed the calculation of perforation skin factor, the calculation of the damage zone skin factor, and the calculation of the crushed zone skin factor. In our calculation we neglected the value of the other parameters skin such the completion skin due to the

1.375

210.559

1.37042

Oil formation volume factor (bbl/STB)

Reservoir permeability (mD)	243
Well radius (ft)	0.292
Drainage radius (ft)	4641.2
Average Formation Porosity	0.25
Perforation interval (ft)	4.92
Rock compressive strength (calculated, psia)	4217.39
Perforation tunnel diameter for the different guns $(1,2,3,4)$ (in)	0.30, 0.29, 0.30, 0.28
Perforation phasing , (°)	60
Shot density (shots/ft)	6

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# Table 5 The B

partial penetration (S<sub>c</sub>), and the outer boundary geometry skin (S<sub>A</sub>), as well the gravel-pack skin (S<sub>G</sub>) because our work was considering on the effect of the perforation skin. In our work we calculate the perforation skin effect by using Karakas and Tariq method because the other methods were not including all the phasing angles. To calculate the perforation skin effect by using Karakas and Tariq method, we consider the equations number (13, 14, 15, 16, 17, 18, 19, 20, 21, and 22). In our work we made calculation steps as following:

- I. Calculation the penetration depth.
- Calculation the Perforation Skin Effect by using Karakas and Tariq method.
- III. Calculation the effect of a crushed zone skin factor.
- IV. Calculation the composite skin factor.
- V. Calculation the flow rate.

In this work, we calculated the perforation damage zone skin factor using the equation number (3) considering the damage zone permeability and damage zone radius; first we calculated all parameters of the well number 1 to get the flow rate.

# Calculate the penetration depth $(L_p)$

To calculate the penetration depth we must know the compressive **Table 9** The Results of Perforation Depth Calculation for Well I

# strength of the formation oil well. We used Thompson correlation (eq 8) to calculate the penetration depth, and the data from the (Table 4) (Table 8). We have to determine the effective compressive strength which is equal to the overburden pressure minus the formation pressure. The overburden can be estimated by multiplying depth by the overburden gradient of 1.1 psi/ft. the formation pressure is the reservoir pressure at the time of perforating.

Table 8 Required Data to Calculate the Compressive Strength

Data	Value
Berea compressive strength (CB)	6500 psia
Perforation Depth interval	From 5789.2 to 5795.76
Cement sheath thickness (TS)	Usually 0.75 in
Casing thickness (TC)	Usually 0.375 in

The overburden pressure=[1.1 psi/ft\*(average perforation depth ft)].

Average perforation depth ft.=((5789.2+5795.76) / 2) ft

Compressive strength  $psiz = [1.1 psi/ft^* (average perforation depth ft)-(the formation pressure psia)]. Table 9 shows the calculation results of perforation depth.$ 

Number of gun	Phasing	Shots (spf)	Compressive	Total target penetration (in)	Perforation depth
	(°)		strength ( Pisa)		( in )
I	60	6	4125.548	19.2	22.425
2	60	6	4125.548	20.6	24.142
3	60	6	4125.548	22	25.859
4	60	6	4125.548	26	30.765

# Calculate the perforation skin effect by using karakas and tariq method

We choose this method instead of the other methods because in this method we can calculate the perforation skin factor of the phasing angle  $60^{\circ}$  and 6 shots per feet.

Table 10 Calculation Results of the Flow Pseudo Skin Factor  $(S_h)$  for Well I

# Calculation of the flow pseudo skin factor $(S_h)$

We used equation (14) to calculate  $(S_h)$ . We calculated the effective wellbore radius as function of the phasing angle (60°) from the equation (15). We used table 1 to determine a phase dependent variable ( $\alpha \theta$ ). Table 10 shows the calculation results of the flow pseudo skin factor  $(S_h)$ .

No	Phasing (°)	Shots (spf)	r <sub>w</sub> (ft)	L <sub>p</sub> (in)	αθ	r <sub>w</sub> (θ)	S <sub>h</sub>
I	60	6	0.292	22.425	0.813	18.468	-4.147
2	60	6	0.292	24.142	0.813	19.865	-4.219
3	60	6	0.292	25.859	0.813	21.26	-4.287
4	60	6	0.292	30.765	0.813	25.249	-4.459

# Calculate the vertical pseudo skin factor (S)

We used equation (19) to calculate  $(S_v)$ . To calculate  $(S_v)$  we must calculated certain dimensionless variables. We Calculated  $(h_D)$  by using equation 16. We Calculated  $(r_{pD})$  by using equation (17). We Calculated the values a, b, by using equations 20, and 21. The

constants values  $a_1$ ,  $b_1$  are given in the Table 2 as function of the phasing angle (60°). By using all the parameters that we calculated in the different shapes, we can determine the vertical pseudo skin effect ( $S_v$ ). Table 11-14 shows calculation results of the vertical pseudo skin factor (S\_).

**Table 11** Calculation Results of the Dimensionless Variable  $(h_D)$  for Well 1

No	Phasing (°)	Shots (spf)	h (ft)	L <sub>p</sub> (in)	$\mathbf{k}_{\mathrm{h}}^{\prime} \mathbf{k}_{\mathrm{v}}^{\prime}$	h <sub>D</sub>
I	60	6	0.167	22.425	5	0.016
2	60	6	0.167	24.142	5	0.015
3	60	6	0.167	25.859	5	0.014
4	60	6	0.167	30.765	5	0.012

Table 12 Calculation Results of the Dimensionless Variable  $(r_{_{pD}})$  for Well I

No	Phasing (°)	Shots (spf)	L <sub>p</sub> (in)	$\mathbf{k}_{\mathrm{h}}^{\prime}/\mathbf{k}_{\mathrm{v}}$	r <sub>perf</sub> (in)	r <sub>p</sub> D
I	60	6	22,425	0.2	0.3	0.036
2	60	6	24,142	0.2	0.29	0.035
3	60	6	25,859	0.2	0.3	0.036
4	60	6	30,765	0.2	0.28	0.034

Table 13 Calculation Results of the Constants a and b for Well I

No	Phasing (°)	Shots (spf)	а	b
I	60	6	1.629	3.05
2	60	6	1.636	3.049
3	60	6	1.629	3.05
4	60	6	1.644	3.048

# Calculate the wellbore skin factor $(S_{wb})$

 $S_{wb}$  can be determined by using equation (22), and the constants  $c_1, c_2$  can be obtained from Table 3, the value  $(r_{WD})$  from the equation (18). Finally we can determine the perforation skin effect  $(S_p)$  by using the equation (13). Table 15 calculation results of the wellbore skin factor  $(S_{wb})$  and Table 16 shows the calculation results of the perforation skin effect  $(S_p)$ .

 Table 15 Calculation Results of the Wellbore Skin Factor (S<sub>wh</sub>) for Well 1

Table 14 Calculation Results of the Vertical Pseudo Skin Factor (S.) for Well I

No	Phasing(°)	Shots(spf)	(S <sub>v</sub> )
I	60	6	3.84E-04
2	60	6	3.05E-04
3	60	6	2.86E-04
4	60	6	1.71E-04

 Table 16 Calculation Results of the Perforation Skin Effect ( $S_p$ ) for Well 1

No	Phasing(°)	Shots(spf)	S <sub>h</sub>	S <sub>v</sub>	S <sub>wb</sub>	SP
I	60	6	-4.147	3.83E-07	0.000375	-4.146
2	60	6	-4.219	3.05E-07	0.000369	-4.219
3	60	6	-4.287	2.86E-07	0.000364	-4.287
4	60	6	-4.459	1.71E-07	0.000353	-4.459

# Calculate the effect of a crushed zone skin factor $(S_{dp})$

By using the equation (9) and the data in in Table 4 we can determine  $(S_{dp})$ . We determine the following:

Total number of perforation (N)=Shots (spf) \* Perforation interval  $(h_n)$  ft. N=6\*6.56=39.36 shots.

Perforation radius  $(r_p)$  and the Crushed zone radius  $(r_{dp})$  are given from the Table 17. We assumed that the  $k_a = k_o/5$  that usually in Hungarian oil well. Table 18 shows the Calculation Results of crushed zone skin factor (Sdp). Table 18 shows the calculation results of crushed zone skin factor (Sdp).

Table 17 Show the Perforation Radius  $(r_{_{\rm P}})$  and the Crushed Zone Radius  $(r_{_{\rm d}})$  for Well I

No	Perforation radius (In)	Crushed zone radius(In)
I	0.15	0.65
2	0.145	0.645
3	0.15	0.65
4	0.14	0.64

					( wb	
No	Phasing(°)	Shots(spf)	r <sub>"</sub> (ft)	L <sub>p</sub> (in)	r <sub>wD</sub>	S <sub>wb</sub>
I	60	6	0.292	22.425	0.013	0.000375
2	60	6	0.292	24.142	0.012	0.000369
3	60	6	0.292	25.859	0.011	0.000364
4	60	6	0.292	30.765	0.009	0.000353

Evaluation of the productivity of vertical oil wells by using different high shot density (HSD) guns

No	kॢ(mD)	k <sub>a</sub> (mD)	r <sub>a</sub> (ft)	r <sub>w</sub> (ft)	k <sub>dp</sub> (mD)	h <sub>p</sub> (in)	L <sub>p</sub> (in)	S <sub>p</sub>	<b>S</b> <sub>dp</sub>
I	169	33.8	1.375	0.292	5	6.56	22.4247	-4.1467	3.766428
2	169	33.8	1.375	0.292	5	6.56	24.14187	-4.21958	3.56099
3	169	33.8	1.375	0.292	5	6.56	25.85903	-4.2875	3.266209
4	169	33.8	1.375	0.292	5	6.56	30.76522	-4.45946	2.845485

Table 18 The Calculation Results of Crushed Zone Skin Factor  $(S_{do})$  for Well I

# Calculate the composite skin factor (S)

We used equation (11) to determined (S). In our calculation we considered the effect of the perforation skin factor, and the crushed zone skin factor, thus we calculate the damage zone skin factor. In our calculation we suggest that the completion skin factor is equal zero, but if we consider the value of the completion skin factor like (10), we will have the lower flow rate. We calculated the value of the damaged zone skin factor from the equation (3), thus we used the data in the Table 4. Table 19 shows the calculation results of the skin factor (S).

Figure 1 shows the relationship between the perforation depth and the skin factor, considering the theoretical overview as you can see in the figure and this is favorable for us because the deeper perforation the lower skin factor. Figure 2 shows the relationship between the perforation depth and the flow rate. The flow rate increased with the increasing of the perforation depth.

$$S_{2}=(169/33.8-1) \ln (1.375/0.292)$$

Table 19 The Calculation of the Skin Factor (S) for Well I

No	S <sub>P</sub>	h (ft)	h <sub>P</sub> (ft)	h/ h <sub>P</sub>	Sa	<b>S</b> <sub>dp</sub>	S
I	-41,467	262,467	6,56	4,001,021	7,98	3,766,428	1,911,743
2	-421,958	262,467	6,56	4,001,021	7,98	356,099	1,862,041
3	-42,875	262,467	6,56	4,001,021	7,98	3,266,209	1,805,387
4	-445,946	262,467	6,56	4,001,021	7,98	2,845,485	1,694,516



Figure I The Relationship between Perforation Depth and Skin Factor for Well.

# Calculate the flow rate q<sub>o</sub> (bbl/day)

We used the equation (1) to calculate the flow rate considering the total skin factor that we calculated in the step 4, thus the data from the Table 4. I released that the lower skin factor (S) the higher flow rate  $(q_o)$  as you can see in the Table 20 as well as Figure 3. As well you can see the best type of gun to have the higher productivity is the gun 4, with deeper perforation depth. The Figure 3 shows the relationship between the skin factor and the flow rate, as you can see increasing of skin factor decreasing of the flow rate.

Table 2	20 The	Calculation	Results	of the	Flow	Rate g	(bbl/day)	for Well	L
						1000	(		

No	L <sub>p</sub> (in)	S	q。
Gun I	22.4247	19.11743	179.3193
Gun2	24.14187	18.62041	182.547
Gun3	25.85903	18.05387	186.3709
Gun4	30.76522	16.94516	194.3376
-			



Figure 2 The Relationship between Perforation Depth and Flow Rate for Well I.



Figure 3 The Relationship between Skin Factor and Flow Rate for Well 1.

# Calculate the flow rate of the other wells

We followed the steps that we used to calculate the different parameters in the well 1 to determine the skin factor and flow rate of all the other wells.

For well 2: Our work in well 2, considering the parameters in the Table 21-23. The final result that we got in the Table 23 is the flow rate of the well 2 by using different kind of guns. As you can see in our work the best flow rate was at using the gun 4, herein in this well we retested that the flow rate quiet low because of the interval perforation was so small. In this case, we recommended to perforate with high **Table 21** The Calculation Results for the Perforation Depth for Well 2

interval perforation length to get more increasing flow rate. As you can see, Figure 4 shows the relationship between the perforation depth and the skin factor, and Figure 5 shows the relationship between the perforation depth and the flow rate. Figure 6 shows the relationship between the skin factor and the flow rate.

Number of gun	Phasing	Shots (Spf)	Compressive	Total target penetration(In)	Perforation depth
	(°)		strength ( Pisa)		( In )
I	60	6	4094.174	19.2	22.48833
2	60	6	4094.174	20.6	24.21013
3	60	6	4094.174	22	25.93194
4	60	6	4094.174	26	30.85138

Table 22 The Calculation Results for the Skin Factor (S) for Well 2

No	S <sub>P</sub>	h (ft)	h <sub>P</sub> (ft)	h/ h <sub>P</sub>	Sa	<b>S</b> <sub>dp</sub>	S
I	-4.1495	19.685	3.28	6.001524	7.93	5.017458	27.72193
2	-4.22237	19.685	3.28	6.001524	7.93	4.660621	26.92777
3	-4.29029	19.685	3.28	6.001524	7.93	4.35E+00	26.21071
4	-4.46223	19.685	3.28	6.001524	7.93	3.66E+00	24.48499

Table 23 The Calculation Results for the Flow Rate  $q_0$  (bbl/day) for Well 2

No	L <sub>P</sub> (in)	S	q <sub>o</sub> (bbl/day)
I	22.48833	27.72193	24.56318
2	24.21013	26.92777	25.10833
3	25.93194	26.21071	25.62176
4	30.85138	24.48499	26.94794



**Figure 4** The Relationship between Perforation Depth and Skin Factor for Well 2.

**For well 3:** Our work in well 3, considering the parameters in the Table 24-26. Table 24 shows the results of our calculation of the different parameters of the well 3 by using the same steps in the well 1. As you can see the final results was the calculation of the flow rate. Figure 7 shows the relationship between the perforation depth and the skin factor and Figure 8 shows the relationship between the perforation shows the relationship between the skin factor and the flow rate.



Figure 5 The Relationship between Perforation Depth and Flow Rate for Well 2.



Figure 6 The Relationship between Skin Factor and Flow Rate for Well 2.

**For well 4:** Our work in well 4, considering the parameters in the Table 27-29. Table 29 shows the final result of our calculation of well 4, in our work of this well, we released that the influence of the skin factor not too much because the influence of the oil permeability more than the skin factor the permeability is high in this well. As you can see, Figure 10 shows the relationship between the perforation depth

and the skin factor and Figure 11 shows the relationship between the perforation depth and the flow rate. Figure 12 shows the relationship between the skin factor and the flow rate. After our calculation of the well 2 and well 3 and well 4 by using the same steps that we did in **Table 24** The Calculation Results for the Perforation Depth for Well 3

well 1, we determine the influence of perforation depth and the skin factor with the flow rate. Thus the best gun that we recommended is by using gun 4. If we used gun 4 for these wells we will increased the oil production will higher penetration into the formation zone.

Gun number	Phasing	Shots (spf)	Compressive	Total target penetration (in)	Perforation depth
	(°)		strength (Pisa)		(in)
Ι	60	6	4217.39	19.2	22.23943
2	60	6	4217.39	20.6	23.94309
3	60	6	4217.39	22	25.64674
4	60	6	4217.39	26	30.51433

Table 25 The Calculation Results for the Skin Factor (S) for Well 3

No	S <sub>P</sub>	h (ft)	h <sub>P</sub> (ft)	h/ h <sub>P</sub>	Sa	S <sub>dp</sub>	S	
I	-4.13851	4.9213	4.92	1.000264	7.91	5.749455	9.521972	
2	-4.21141	4.9213	4.92	1.000264	7.91	5.340356	9.039958	
3	-4.27935	4.9213	4.92	1.000264	7.91	4.985608	8.617251	
4	-4.45134	4.9213	4.92	1.000264	7.91	4.190313	7.649917	

Table 26 The Calculation Results for the Flow Rate qo (bbl/day) for Well 3

No	LP (in)	S	q <sub>o</sub> (bbl/day)
I	22.23943	9.521972	52.55092
2	23.94309	9.039958	53.961
3	25.64674	8.617251	55.26137
4	30.51433	7.649917	58.48674



Figure 7 The Relationship between Perforation Depth and Skin Factor for Well 3.



Figure 8 The Relationship between Perforation Depth and Flow Rate for Well 3.



Figure 9 The Relationship between Skin Factor and Flow Rate for Well 3.



Figure 10 The Relationship between Perforation Depth and Skin Factor for Well 4.

# Evaluation of different guns and influence of it

The aim was to compering the effect of the guns for the flow rate of each well. We made relationship between the flow rate and perforation depth with different kind of guns, and we found the influence of the effected guns with the perforation depth of all oil vertical wells. This relationship was shown in the Figure 13-16. Table 30-33 and figures 13 through 16 show the effect of gun 1, 2, 3, and 4 with different oil vertical wells. Highest flow rate that we can see was in the well 4 and the lowest flow rate was in well 2.



Figure 11 The Relationship between Perforation Depth and Flow Rate for Well 4.

Table 27 The Calculation Results for the Perforation Depth for Well 4



Figure 12 The Relationship between Skin Factor and Flow Rate for Well 4.

Gun number	Phasing	Shots (Spf)	Compressive	Total target penetration (In)	Perforation depth
	(°)		strength (Pisa)		(In)
I	60	6	4101.885	19.2	22.47267
2	60	6	4101.885	20.6	24.19334
3	60	6	4101.885	22	25.914
4	60	6	4101.885	26	30.83018

Table 28 The Calculation Results for the Skin Factor (S) for Well 4

No	SP	h (ft)	h <sub>P</sub> (ft)	h/ h <sub>P</sub>	Sa	S <sub>dp</sub>	S	
Ι	-4.58986	193.59	32.8	5.902134	10.14	7.835891	40.61719	
2	-4.66306	193.59	32.8	5.902134	10.14	7.278592	39.6279	
3	-4.73126	193.59	32.8	5.902134	10.14	6.795301	38.74208	
4	-4.90383	193.59	32.8	5.902134	10.14	5.711722	36.63994	
								-

Table 29 The Calculation Results for the Flow Rate qo (bbl/day) for Well 4

No	LP (in)	S	q <sub>o</sub> (bbl/day)
I	22.47267	40.61719	486.7441
2	24.19334	39.6279	496.7768
3	25.914	38.74208	506.1177
4	30.83018	36.63994	529.7562



Figure 13 The Relationship between Perforation Depth and Flow Rate for Gun I.



Figure 14 The Relationship between Perforation Depth and Flow Rate for Gun2.

# Comparing between the different high shot density Guns

Comparing between the results of the flow rate and perforation depth by using different high shot density Guns. Figure 17 shows the comparing of the flow rate with different kind of guns. The higher

flow rate we can have with selecting the gun 4 with higher perforation depth, the lower flow rate we can see with choosing the gun 1 with lower perforation depth. The main conclusion belonging to the Figure 17, each gun gives the highest flow rate at well 4, but comparing the effect of the guns as you can see, this is dependent on the perforation depth and the compressive strength of the layers because the well test shows well 4 has the highest interval perforation of two sections. The deeper perforation that we got by using gun 4 with highest API RP 43 penetrations, that we got from the Schlumberger engineered perforation systems. The flow rate as you can see in the Figure 17 is slightly increasing of all the guns. We consider the damage zone thickness of all the wells are the same, if it not the same property will shot through the damage zone might be different by using the different kind of high shot density guns.



Figure 15 The Relationship between Perforation Depth and Flow Rate for Gun3.



Figure 16 The Relationship between Perforation Depth and Flow Rate for Gun3.

No	L <sub>P</sub> (in)	S	q <sub>o</sub> (bbl/day)
3	25.64674	8.617251	55.26137
I	25.85903	18.05387	186.3709
4	25.914	38.74208	506.1177
2	25.93194	26.21071	25.62176

Table 31 The Calculation Results for the Flow Rate q (bbl/day) for Gun2

No	L <sub>P</sub> (in)	S	q <sub>o</sub> (bbl/day)
Well 3	23.94309	9.039958	53.961
Well I	24.14187	18.62041	182.547
Well 4	24.19334	39.6279	496.7768
Well 2	24.21013	26.92777	25.10832

Table 32 The Calculation Results for the Flow Rate  $q_0$  (bbl/day) for Gun3

Νο	L <sub>P</sub> (in)	S	q <sub>o</sub> (bbl/day)		
Well 3	22.23943	9.521972	52.55092		
Well I	22.4247	19.11743	179.3193		
Well 4	22.47267	40.61719	486.7441		
Well 2	22.48833	27.72193	24.56318		
	No Well 3 Well 1 Well 4 Well 2	No         L <sub>P</sub> (in)           Well 3         22.23943           Well 1         22.4247           Well 4         22.47267           Well 2         22.48833	No         L <sub>p</sub> (in)         S           Well 3         22.23943         9.521972           Well 1         22.4247         19.11743           Well 4         22.47267         40.61719           Well 2         22.48833         27.72193		

Table 33 The Calculation Results for the Flow Rate q. (bbl/day) for Gun4

No	L <sub>P</sub> (in)	S	q <sub>o</sub> (bbl/day)	
3	30.51433	7.649917	58.48674	
I	30.76522	16.94516	194.3375	
4	30.83018	36.63994	529.7562	
2	30.85138	24.48499	26.94794	



Figure 17 The Comparison between Flow Rate Results While Using Different Kind of High Shot Density (HSD) Guns.

# Conclusion

The first conclusion as we prove in this work that there is a calculation method by which the flow rate of the vertical oil wells can be estimated before perforating. To have the best flow rate the right design of the guns we should choose. The most important parameters influence the productivity of the perforated oil vertical wells are (penetration depth, perforation diameter, shot density, and phasing angular). In this work we evaluate the productivity of four selected wells in Hungary field, the main results of our evaluation are listed below:-

- a. The perforation depth based on the compressive strength of the layer (the higher compressive strength the lower perforation depth).
- b. The perforation skin factor based on different skin effect like (flow pseudoskin factor, vertical pseoduskin factor, wellbore skin factor).
- c. The crushed zone skin factor based on (formation permeability, crushed zone permeability, damage zone permeability, perforation interval, perforation radius, crushed zone radius, perforation depth).
- d. The skin factor based on (crushed zone skin factor, perforation skin factor, damage zone skin factor, perforation interval).
- e. The flow rate based on the total skin factor and other parameters like (reservoir properties, flow properties, well radius, Drainage radius).

The longer perforation interval the higher flow rate that can be obtained. In this work we couldn't use the rearranged Harris handy charts by standing for calculation of the perforation skin factor because it is not including the all phasing angle and the shot density. In this work we used high shot density guns with phasing angle  $(60^{\circ})$  and we got a good result by using some MOL company data. Depending on our results, we recommend using these guns to have higher flow rates. Finally this kind of Hungarian wells would give the highest production rate if it perforated with high shut density guns, the best results if these wells perforated with gun 4.

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# **Conflict of interest**

The authors declare no conflict of interest.

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