

Appendix 1

1-full conditional distribution for σ_e^2 :

$$\sigma_e^2 | \theta_{(-\sigma_e^2)}, \mathbf{y}_{obs}, \mathbf{t} \sim I\Gamma(\alpha_{\sigma_e^2}, \tau_{\sigma_e^2}),$$

$$\text{where, } \alpha_{\sigma_e^2} = \frac{\sum_{i=1}^n n_i}{2} + \tau_e \text{ and } \tau_{\sigma_e^2} = \frac{1}{T_e} + \frac{1}{2} \sum_{i=1}^m (\mathbf{y}_i - \mathbf{x}'_{1i} \boldsymbol{\beta}_1 - \mathbf{z}'_{1i} \mathbf{b}_{1i})' (\mathbf{y}_i - \mathbf{x}'_{1i} \boldsymbol{\beta}_1 - \mathbf{z}'_{1i} \mathbf{b}_{1i})$$

2-full conditional distribution for $\boldsymbol{\Psi}_k$, k=1,2:

$$\pi(\boldsymbol{\Psi}_k | \boldsymbol{\theta}_{(-\boldsymbol{\Psi}_k)}, \mathbf{y}, \mathbf{t}) \sim IW_{q_k} \left[(m + \tau_{b_k}, \mathbf{T}_{b_k}^{-1}) + \sum_{i=1}^m s_{b_{ik}}^2 (\mathbf{b}_{ik} - \mathbf{D}_{b_k} \mathbf{W}_{b_{ik}} + \boldsymbol{\mu}_{b_k}) (\mathbf{b}_{ik} - \mathbf{D}_{b_k} \mathbf{W}_{b_{ik}} + \boldsymbol{\mu}_{b_k})^T \right]$$

3-full conditional distribution for $\mathbf{S}_{b_{ik}}^2$, k=1,2:

$$\pi(\mathbf{S}_{b_{ik}}^2 | \boldsymbol{\theta}_{(-\mathbf{S}_{b_{ik}}^2)}, \mathbf{y}, \mathbf{t}) \sim G(\alpha_{0k}, z_{0k})$$

$$\alpha_{0k} = \frac{2q_k + v_{b_k}}{2} \text{ and } z_{0k} = \frac{v_{b_k} + (v_{b_k} + \mathbf{w}_{b_k}^T \mathbf{w}_{b_k}) + (\mathbf{b}_{ik} - \mathbf{D}_{b_k} \mathbf{W}_{b_{ik}} + \boldsymbol{\mu}_{b_k})^T \boldsymbol{\Psi}_k^{-1} (\mathbf{b}_{ik} - \mathbf{D}_{b_k} \mathbf{W}_{b_{ik}} + \boldsymbol{\mu}_{b_k})}{2}$$